

**BIFURCATIONS WITH MULTI-DIMENSIONAL KERNEL IN A  
CHEMOTAXIS-GROWTH SYSTEM**

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**ABSTRACT.** We study the bifurcation problem for a chemotaxis-growth system with logistic growth in a two-dimensional rectangular domain. We apply the local bifurcation theorem by Ambrosetti and Prodi that does not require one-dimensional degeneration of the linearized operator around trivial solutions. We then obtain bifurcation solutions with two- and three-dimensional degeneration indicating spatially regular nesting patterns.

*Key words and phrases.* chemotaxis-growth system, Lyapunov-Schmidt reduction, bifurcation, codimension-two bifurcation, codimension-three bifurcation.

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